

No. *Aitbrey* THE ~~Book~~ XIX

NEVV ARTIFI- CIAL GAVGING LINE OR ROD:

Together with rules concerning
the use thereof:

Invented and written by WIL-
LIAM OUGHTRED,
who

In all due and respective observance
præsenteth the same

To the Right Honourable LL. Sir NICOLAS
RAINTON Lord Major of London for
this præsent yeare, and RALPH
FREEMAN Alderman Lord
Major elect for the yeare
now ensuing.
and

To the Worshipfull GEORGE ETHRIDGE
late Master, and CAPTaine JOHN MILLER
the præsent Master of the Company
of Vintners.

And to the whole body of that Right
Worshipfull Societie.



London Printed by *Aug. Mathewes.* 1633.

*ex dono Benjamin Oughtredi.
auctoris filij.*

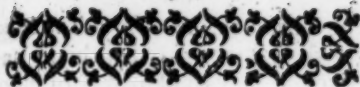
XIX

Lum Go: Aubry R.S.S.

Donu Benjam: Cugherdi

Fil. Antori.

1793: 673.



Right Honourable,
and
Right Worshipfull.

I Doubt not, but as every
worthy and laudable
worke is subject to ob-
loquie and ill constru-
ction: So this my good
intent and usefull invention, which I
here present unto you Right Honour-
able Lords, and you Right Worship-
full, into whose clientlie I betake
both my selfe and it, shall meet with
some over-curious and supercilious
censurers, who will misse-judge and
misse-say the same: though not for
theart (against which I perswade
my selfe they shall find little cause to
except) yet in respect of my particu-
lar calling: of the height and dig-
nity whereof, such small and low co-
gitations may seeme to be unworthy.
But may it please them to consider,
A 2 that

that Theologie is *ἐπιστήμη μάλιστα ἀρχι-
 νική καὶ ἀρχιτεκτονική*, the chiefe and
 principall Lady and Mistresse of all o-
 ther faculties; unto which all callings
 in this life, for their just, faithfull, and
 conscionable execution, are to com-
 ply, and bee accountable. And seeing
 God in his sacred word biddeth not
 onely *cease to doe evill*, but also *learn
 to doe well, and seeke judgement*; that
 Divine may bee thought best to per-
 forme his durie; that shall not onely
 reprove injustice and wrong dealing,
 but shall also even in particular acti-
 ons informe the conscience both what
 is right, and how to performe it. This
 I have herein endeavoured to effect.
 The holy Scripture is frequent in
 shewing the abomination of false and
 deceitfull weights; and in forbidding to
 doe unjustly in line, in weight, or in mea-
 sure: and telleth us that a true weight,
 and a just balance are of the Lord; and
 that all the weights in the bagge are his
 worke. If I therefore by the helpe of
 God, and the knowledge hee hath
 beene pleased to give me, shall exhi-
 bite

Esa. 1. 16.

Mic. 6. 11.
 Lev. 19. 35.
 Prov. 16.
 11.

bire unto this renowned Citie, a line and rule to measure vessels with according to true art, and shall teach how to reforme an error, which hath for some time (through ignorance of better) usurped the place of truth; and that with much more facility, then it is committed: I hope I shall not justly be thought to wander out of the limits of my profession and calling. Now the occasion whereby I invented it was this.

Many yeares agoe, I devised for my private use an instrument, which I called *the Circles of proportion*: which is nothing else but *the Logarithmes of Numbers, Sines, and Tangents* set on circles. And I writ in latine the manifold uses thereof, not onely in *Arithmetical; Geometrical, and Astronomical calculations*, but also in divers other accounts, practises, and questions, which are occurrent in the civill societie and conversation of mankind: among which one was concerning *the measuring or Gauging*

The occasion vvhether by this gauging instrument was invented.

of vessels : wherein taking the forme of them to be *spharoides, or like a long sphere*, with the two ends equally cut off, (as generally both by the ancienter and later writers is supposed, and in the fabric of such vessels is still aymed at by the Makers) I delivered out of the grounds and inventions of that most admirable Artist *Archimedes*, the true and artificiall way of finding their severall contents : and applyed it unto the use of that my instrument, with as much ease and expeditnesse as I could. Neither did I at all discourse upon the Mechanicall wayes practised by other men, much lesse refute any of their errors, but onely barely and positively delivered the truth. These my notes, and that my instrument (after many yeares) at the perswasion of a friend of mine, who profered to translate them into English, I was content he should set out and make common, my selfe not having any hand in that publication. When now the translation was ready for the Printer, my friend

friend having perused that which *Master Gunter* in his second booke of the *Crosse staffe Chapt. 4.* writeth very obscurely about Gauging of vessels, asked mee what he meant by the *meane Diameter* after the vsuall manner? I answered him that in the vsuall manner of art there was no *medium* or *meane*, but the *meane* betweene the two extreme termes in some kind of Proportion: and that all proportion being either *Arithmetical*, *Geometrical*, or *Musical*, hee being a Scholer and an Artist, must needs (as I thought) by the *meane* understand one of those three: and most likely the *meane arithmetical* which is the greatest of them. For supposing the two extreme termes to bee 9 and 4, betweene these the *meane arithmetical* is 6½, which is halfe the summe of both: the *meane geometrical* is 6: and the *meane in musical proportion* is 5⅔. And yet said I, the *meane arithmetical* is too little, as in the mensuration of tapering timber I proved: much more either of the

two rest. And other meane diameter, which may give the true content of a sphaeroides, art affordeth none. My friend replyed, Master *Gunter* is generally acknowledged to have bin a man of skill, and you utterly unknowne: and hee that shall find your booke, disagreeing from his documents, will without any more adoe reject it; you shall therefore doe well to write in a few lines why you differ from M^r. *Gunter*, and to shew that his way by the meane diameter cannot stand with art. Which his counsell I seeing not to be unnecessary, especially in regard of the great paines hee had taken in the translation of my notes, tooke a pen, and presently in the margin of his translation writ that short advertisement touching M^r. *Gunters* meane diameter.

Not long after that translation was in print, word was sent me into the countrey, that an old man (that said he was) *the Gauger of London* came earnestly inquiring after me, and was very angry; professing hee would vindicate

dicare Mr. Gunters credit, and speake for him, that could not answer for himselfe: and that I had taught a false way of Gauging vessels: and that both hee and many others, had bought of my bookes; which much troubled him: and hee was very solicitous how they should come by their money againe: and that hee never saw such a booke in his life; for he could not tell what to make of it. The translator told him, that when he, or any other for him, should disprove that way of measuring vessels, which I had delivered; let him bring his booke, and he should have his money againe for it.

At my next comming to London, hee hearing of my being in towne, came to mee, and expostulated with me, why I would presume to question any thing that Mr. Gunter writ? I answered him, that it is a fault incident to the students of these arts, to be very incredulous, especially if they see demonstration to the contrary. Hee said I understood not what Mr. Gunter meant by the meane diameter after

after the vsuall manner : For Mr. Gunter (though hee said not so much) did understand the manner vsuall in London ; and that hee himselfe followed in gauging : which was to halfe the summe of the diameters at the head and bung, and to adde one quarter of their difference : and that this was a true way, and a better way then mine : and that if hee should use my way, it would require much more paines, and longer time : and that hee had a man, whom hee had taught, which had little or no skill in Arithmetick, and could scarce multiply, yet in his way hee should gauge with any man in England ; and that if that his way were not right, hee might doe more wrong in a few yeares then any Aldermans state in London is worth ; and that hee was sworne to doe justly. I answered, that the greater tye lay upon him to doe justly, and the more hurt hee might doe by misgauging, the more thanks hee owed mee, for shewing him the right ; and with the more gladnesse hee should embrace it, notwithstanding it might have

have some more difficultie : for though I should hold my peace (as Mr. Gunter it seemeth did) yet hee were never the more justifiable: and wished him to looke to his conscience : especially seeing now hee might informe himselfe in the truth. Hee said hee found indeed by his experience, that the adding of a quarter of the difference was somewhat too much ; and therefore that now hee began to take one fift part thereof : and yet both wayes were better then mine ; and hee would not learne of mee to gauge vessels. And so went his way in great choler and displeasure. I did indeed wonder at that his assertion; that whether hee tooke the quarter, or the fift part of the difference, yet both are better then the way of art, which I had delivered : for even in that example, which in my booke is set downe, of a vessel having the diameter at the bung 32 inches, and the diameter at the head 18 inches, and the length 40 inches; had hee but made triall, hee should have found the
content

content computed by one quarter of the difference, to have beene gallons 110 and almost an halfe; and by one fift part, to have beene gallons 105 $\frac{1}{2}$; whereas the true measure by art is gallons 107 and an halfe and somewhat better; which is almost in the very midst betweene both: so that if any man will suppose one of his wayes, bee it the former, or the latter, to bee right: yet the other must of necessitie bee further from the truth, then that which I taught; because it falling betweene both, must needs bee neerer to each, then one of them is to the other.

Not long after *Mr. Elias Allen* (a man well knowne and esteemed by all men of art for his skilfulnesse in making instruments in metal) being in the company of some gentlemen of good quality and worth, upon occasion related these former words of the Gauger, what great detriment hee might doe by his manner of Gauging, if it were not true. Which his speech *Mr. George Eshrege*, then Master of the

the right worshipfull Company of
Vintners, hearing and observing, said
 that indeed he doubted not, but there
 was much wrong done by misgauging
 wine vessels ; and that many times
 they found it to their cost ; but they
 could not easily remedy it. And there-
 fore invited Mr. *Allen* to request me to
 devise a *Gauging instrument*, which
 might be according to true art, and of
 familiar and easie performance; that
 they might examine and try their
 vessels themselves : and said it would
 bee an invention very acceptable, and
 of great use, and a meanes to prevent
 much wrong that many times is done.
 Which inquisition and studie, to find
 out a true and perfect instrument for
 measuring of vessels (though at first
 without any hope of effecting any
 singular thing therein after such a num-
 ber of learned artists, and writers in
 this kind, with the meanest of which
 I am not to bee compared). I under-
 tooke, merely out of my love to the
 society of mankind, and my desire of
 advancing truth and justice ; and at
 last

last by the helpe of God, who is righteous, and loveth righteousness, have brought to passe : And herein withall humble and affectionate serviceableness, both unto you my *right honorable LL.* upon whom the principall care of all such admeasurements within this most flourishing and illustrious Citie doth rest, and of you *right worshipfull the Masters and whole Company of Vintners*, and to as many of this most renowned Citie as shall have cause to use the same, I present this my *new gauging instrument*. Onely desiring thus much, that you would be pleased to vouchsafe it your acceptance with the same loving and benevolent respect, as I my selfe had unto you, and the truth, in the investigation thereof.

The tryall made of this gauging instrument : and the certainty of it.

Neither indeed may I omit to report the noble favour that *the right worshipfull Company of Vintners* did afford, though unknowne, unto mee. For when Mr. *Elias Allen* had finished up one of those my *instruments*

organging rods, and had brought it
 to their Hall, they presently deputed
 certaine of their society to see the
 experience and performance thereof,
 at the Taverne by *Leaden-hall* under
 the signe of the *Kings-head*: and
 they tooke the paines to examine the
 truth of it in many and sundry kinds
 of wine vessels; where, as I have
 beenetold (for I was not there pre-
 sent my selfe) beyond all expectation
 they found such an exact agreement
 with the measure of water they filled
 in by gallons, after the sealed Standard
 for wine measure, that in most the
 difference was scarce sensible; where-
 as the markes set thereupon exceeded
 the same measures by two or three,
 and sometimes more then foure gal-
 lons in a vessell. Whereupon they
 agreed with Mr. *Allen* for a price,
 and bespake of him threescore of the
 same my *rods or instruments*. Which so
 noble and courteous respect unto me,
 to decree the examination of that
 my invention (though other be-
 nefit or recompense for the same
 I de-

I demand none) I cannot but acknowledge with much thankfulness.

The facilitie of working by this new rod, compared with the troublesome of the other erroneous way.

Neither is the facilitie of working therewith any whit inferior to the certaintie of it : but even in measuring of vessels by this true rule much lesse paines is taken, then that other erroneous and inartificial way doth necessarily require.

For therein first the two diameters at the bung ; and at the head measured in ynes must be added together, and halfe the summe of them taken and kept.

Secondly the diameter at the head is to bee subdtracted out of the diameter at the bung, and the remaines to bee divided by 4, or else by 5, to find out the quarter, or fift part of their difference.

Thirdly that quarter or fife part of the difference must bee added to the halfe summe kept ; to make up a true diameter.

Lastly there remaineth a proportion to bee wrought by multiplication and division ; which is this,

As

*As the quadrate of 17¹/₁₅ (which Mr
Gunter calleth his gauge point) is
to the quadrate of the meane
diameter last found,*

*So is the length of the vessell measu-
red in inches,
to the content of the same vessell
in wine gallons.*

Such a deale of paines, and such a
multiplicite of worke is undergone
in their ordinary gauging : and yet
when all is done, the capacite or con-
tent of the vessell so found is merely
conjectural ; sometimes falser and
sometimes truer, according as the dia-
meters of the vessell are more or lesse
unequall.

But this way of art, which I pro-
pose, besides that it is constant and uni-
versall in all kinds of wine vessells,
is most easily performed only with
one single addition & multiplication ;
as shall anon bee declared both by
rule, and examples. Soe that now I
hope I have made Mr. Gauger amends

B

for

or the too much difficultie and paines
hee thought my booke put him to;
and that henceforth hee will bee as
earnest to vindicate my credit also,
as hee hath egerly traduced it before
he rightly knew me. For although
I cannot so well excuse his rashnesse
in impertinent interposing himselfe in
questions hee had small skill in: yet
I perswade my selfe he had no malice
against my person, who was then ut-
terly unknowne to him. And for my
part (for ought I remember) I had
not so much as heard of any such offi-
cer about the Citie. But I wholly
impute his offence at me partly to the
high estimation hee had of Mr. Gun-
ter, from whom to dissent he thought
to be a hainous matter: and partly to
his diffidence and distrust of my rule,
how it might hold when it came to
tryal. And therefore I doe willingly
returne againe into favour with him,
and recommend this my invention
and my selfe to his future approbati-
on and friendship; assuring him that
what I have before written was not
intended

intented against him: but onely to shew the true occasion how I fell upon this search and disquisition: which in regard of my profession seemed to bee very necessary.

The principles whereon the way that I teach is grounded, are these two. First that a wine vessell is in forme of a perfect sphæroide with the two ends equally cut off. The truth of which ground appeareth both by the generall consent of almost all who have written of gauging: and by the fabric of such kind of vessels; which by the workemen and makers thereof (so farreforth as in practise they are able) are intended to bee such. And now lately by tryal made thereof with the Standard, whereunto it is found to hold greater correspondence in all kind of those vessels, then could bee hoped for, or almost imagined.

Secondly, that a *sphere, or sphæroide* containeth two third parts of a *cylinder* having the same length and thickness; and consequently that the so-

Two principles or grounds of this gauging instrument.

lid convexitie betweene two cylinders, one within the *spheroide*, and the other without touching it, and having the same center and height, is equall to two third parts of the difference of those two cylinders: which hath long since beene taught by the ancient *Siracusan Archimedes* in his first booke of the *Sphere and Cylinder*, & in his booke of *Cone-like and sphere-like magnitudes*: & of late by our English *Archimedes* Mr Henry Briggs, in his *Treatise of Arithmetica logarithmica*.

The rule of
Gauging
framed out
of those
two
grounds.

Out of the consideration of these two principles, or grounds, I framed my rule, which I set downe in my booke of the *Circles of proportion*, Chapt. 9. in these words. *Measure the two diameters of the vessel, in inches, or else in tenth parts of a foot, the one at the bung hole, the other at the head, and also the length within. And by the diameters found, find out the circles; then adde together two third parts, of the greater circle, and on,*
the 4

third part of the lesse; Lastly, multiply the aggregate by the length: so shall you have the content of the vessell, either in cubic ynches, or cubic tenth parts of a foot. Which afterward in the end of that Chapter (having first inquired the quantity of a gallon both Ale, and Wine measure in solid ynches, the one to bee $272\frac{1}{4}$ the other 231) I taught how to reduce into gallons and hundreth parts, by dividing the whole number of ynches contained in the vessell by either of those two numbers respectively. And this is that very rule, the worke and practice of which I have by art, with an invention not yet thought upon by any other, and with divisions calculated for that purpose, fitted and applied to this my new gauging line or rod.

It consisteth of two rulers of brasfe about 32 ynches of length, which also are halfe an ynh broad, and a quarter of an ynh thick: that being set together they may make halfe an ynh square.

The gauging rod described: and of the severall parts thereof.

At one end of both those rulers are *two little sockets* of brasie fastned on strongly : by which the rulers are held together, and made to move one upon another, and to bee drawne out unto any length, as occasion shall require : and when you have them at the just length, there is upon one of the sockets *a long Scrue-pin* to scrue them fast.

These two little sockets encompasse not both rulers quite round : but have each of them *a slit about a quarter of an ych board* : that they may not hinder the sight of the divisions, which are upon the broad or flat sides of the rulers. Which divisions are indeed of most principall use : being properly the *gauge-divisions* : and are now first of all invented, and accommodated to the mensuration of vessels.

The gauge-divisions are in all two hundred and thirtie : of which every particular division standeth for one hundreth part of a wine gallon : so that they are in all 2 wine gallons and

and 3rd hundred parts. And for the more perspicuous distinguishing of them they are figured by tens thus, 0₁₀, 0₂₀, 0₃₀, 0₄₀, 0₅₀, 0₆₀, 0₇₀, 0₈₀, 0₉₀, 1₀₀, 1₁₀, 1₂₀, 1₃₀, 1₄₀, 1₅₀, 1₆₀, 1₇₀, 1₈₀, 1₉₀, 2₀₀, 2₁₀, 2₂₀, 2₃₀: there being betweene every one of those figures ten divisions, or ten hundredth parts.

At the other end of both the rulers is a *hooke framed into right or square angles* to be serued on: the one with a *Scru-pin*, the other with a *matrix or Scru-plate*. And above these hookes the edge of both rulers is divided into ynces, beginning exactly equall with the ends of the hookes: and figured with 5, 10, 15, 20, 25, 27, 30, &c. And each ynce is subdivided into ten equall parts. Which division of ynces, together with the hookes, serve to take the length of all vessels; that the ends of the barrell boards overreaching the bottoms, may not bee an impediment to the measuring thereof.

Vpon the other edge of each ruler

is set the *the line of Numbers* : which is the very same in both: though some what differently figured. For that on the ruler next the *socket with the long Scrue-pin*, is noted with the figures 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 20, which I therefore call *the line of digit numbers*: and that on the other ruler is figured with tens, as 10, 20, 30, 40, 50, 60, 70, 80, 90, 100, 200, 300: and I call it *the line of denarie numbers*. Wherein you are to remember that from 1 to 5, and from 10 to 50, and also above 100, every space is subdivided into one hundred parts, but above 5 unto 10, and above 50 unto 100, because the spaces are too small to receive an hundred parts, they are subdivided but into fiftie.

The use of
the gauging
rod taught
in foure
rules.

Thus having shewed the description of the severall parts of the *gauging rod*: I now come to the use thereof in measuring any kind of vessel by the wine gallon. For which I will set downe these fower rules,

Rule I.

Rule I. *How to take the length of
a Vessell.*

HAVING first fitted the two
hookes upon the ends of the
two rulers, so that the line of ynches
may be uppermost, draw out the ru-
lers in length, and apply them to the
vessell long wise, so that the two
hookes may embrace the two bot-
toms thereof: at that length scrue
them fast together with the long
Scrue-pin in the socket: then take off
the hooke, which hath the Scrue-pin:
and looke how many ynches the soc-
ket of the ruler which hath the
hooke on doth cut in the ruler with-
out the hooke: for that shall be the
length of the vessell from out side to
out side in ynches: wherefore if out
of that measure you take the thicknes
of the two bottoms (which may bee
easily estimated by a spigot hole) you
shall have the true length of the ves-
sell within.

But if the length of the vessell be
lesse

lesse then 27 ynches, you cannot use both hookes, as before was done. Wherefore apply the ruler which hath the matrix or Scrue-plate to the vessell, setting that hooke against one of the bottoms: and where the divisions of ynches in that ruler beginneth, stick up a knife: then remove that same hooke to the other bottom; and the ynches, which the knife cutteth, shall give the length of the vessell from out side to outside.

Rule II. How to take the Diameters of a Vessell at the Bung, and at the Head, and how to add them together, that you may finde the summe of them.

THe Diameters are not measured by ynches, as the length is, but by Wine gallons, and hundreth parts: in this manner. Take off the hook which hath the scrue-pinne, and dipp that end of the Ruler into the Vessell at the bung; and looke how many parts of the divisions of Gallons t he inside
of

of the bung-hole doth cut, the same shall bee the Diameter at the bung. In like maner apply the same end of the Ruler to the head of the Vessell without; and looke how many parts of the divisions of Gallons it is broad over the midd'st or center thereof; the same shall be the Diameter at the head.

But if the Diameter at the bung be greater then that Ruler is long: draw out the rulers, and setue them at their whole length: and so measure there-with the Diameters, as was before shewed.

The two Diameters being found out must bee added together, thus: Write downe the Diameter at the bung twice, and under it the Diameter at the head onely once, setting like places one under another in the same rowes: that is all the unites in one rowe; all the tenth parts (which are they next the units) in another row; and all the hundreth parts in the last row: and draw a long line betweene the unites and the parts, then adde

adde them all three together into one summe by the way of ordinary Addition. As in example ; Suppose a Vessel that hath the diameter at the bung gallon 1 & 8 hundreth parts, viz. $1\frac{08}{100}$; and the diameter at the head onely 96 hundreth parts of a Gallon, viz. $0\frac{96}{100}$.

you shall write downe
the Diameter at the
bung twice, & the dia-
meter at the head once
and adde them altoge-

$$\begin{array}{r} 1\frac{08}{100} \\ 1\frac{08}{100} \\ 0\frac{96}{100} \\ \hline 3\frac{12}{100} \end{array}$$

ther, as you see done in the side: and the summe of the diameters shall bee found $3\frac{12}{100}$, that is gallons 3 and 12 hundreth parts. And thus shall you doe in all Vessels.

Rule III. *How to multiply the summe of the Diameters of a Vessel by the length.*

THe length of a Vessel being measured in ynches and tenth parts, and the Diameters being found out in Gallons and hundreth parts, and also added together, as hath beene declared

red: The summe of the Diameters is to bee reconed in the line of digit numbers, which is noted with the figures 1, 2, 3, 4, 5, &c. and the length, in the other line of denarie numbers, which is noted with the figures 10, 20, 30, 40, 50, &c. In both which lines of numbers you are to consider, that in the spaces betweene the figures every tenth division is distinguished with a long line: and every single division with a short line: and every fift with a line of a length betweene both. and in the line of digit numbers, they signifie so many handreth parts of a gallon: But in the line of denarie numbers (as also in the line of digit numbers beyond 10) every tenth division is for unites; and every single division is for tenth parts. and beyond 100 every tenth division is for ten, and every single division for one unite. Where note, that in those spaces, which by reason of their smallnesse have but 50, yet they are understood to bee 100, by imagining every one to containe two.

The

The nature and valuation of both the lines of numbers, the digit and the denarie, being understood; multiplication is thus to be wrought. Set the unite place of the line of digit numbers marked with 1, to the place of the length of the Vessell reconed in the line of denary numbers: there set the Rulers fast. then in the line of digit numbers recon the summe of the Diameters found out, that at the Bung being doubled, as was taught before: and looke what space and division it poynteth out in the line of denary numbers: the same being reasonably estimated, shall bee the product sought for.

By estimating reasonably I understand that you consider whether the figure of that space is to bee taken for tens or for hundreds: which is done very easily: for no man is so simple, as to mistake a Vessell of ten or twenty Gallons, for one or two hundred; or of one or two hundred gallons, for one of ten or twenty. And yet this short rule may bee given. That the
product

product is to be estimated according to that former valuation of the line of denarie numbers: unless the Vessel be so small, that the summe of the diameters amount not to one gallon: for then the figures 100 & 200, are to be taken for 10 and twenty.

And if at any time it chance, that the summe of the diameters fallerth not betweene the unite place in the line of digit numbers, and the socket: divide the same summe by 2, and then multiply the one halfe by the length; so shall you have halfe the product sought for: which being doubled will give you the whole.

Rule IIII. How to gauge or measure the content of any Vessel in Wine gallons.

TAKE the length of the Vessel proposed in yench-measure, according to the *Rule I*, then take the two diameters in gallon measure, and adde them together, that at the bung being doubled, according to the *Rule II*.
Lastly

Lastly multiply the summe of the diameters by the length, according to *Rule III*: and the product being reasonably æstimated, shall give the number of Wine gallons contained in that Vessell:

The performance and practice of this Worke by Examples.

Example I.

Diverse examples shewing the use of this Instrument, and the practice of the former rules.

ANd first I will take the Example in my booke of the *Circles of Proportion, Chap 9*, of a Vessell supposed to bee in length 40 ynches; and the diameter at the bung 32 ynches; and the diameter at the head 18 ynches: which two diameters being taken with my gauging rod in gallon measure, would have beene at the bung gallons 1 and 16 hundreth parts, and at the head almost 37 hundreth parts of a gallon. Set downe the diameter at the bung twice, and the diameter at the head once, & adde them: the summe of the

(31)

diameters shall be gallons 2 & almost
 39 hundredth parts, by
Rule II. which being
 multiplyed by 40, the
 product shal be gallons
 107, and better then an
 halfe; which is the true
 content sought for.

$$\begin{array}{r} 1 \overline{) 16} \\ 1 \overline{) 16} \\ 0 \overline{) 37} \\ \hline 2 \overline{) 69} \end{array}$$

Example II. Suppose a small Vessel; whose length is ynches 45 and 3 tenth parts, viz. $45\frac{3}{10}$; and the diameter at the bung 38 hundredth parts of a gallon; and the diameter at the head 30 hundredth parts. what is the content?

Adde the two diameters together, that at the bung being doubled, the summe is gallons 1 and 6 hundredth parts, by *Rule II.* Multiply this summe by the length $45\frac{3}{10}$: and the product shall bee $48\frac{12}{100}$ by *Rule III.*, that is gallons 48 and almost 12 hundredth parts: which is the true content sought for.

$$\begin{array}{r} 0 \overline{) 38} \\ 0 \overline{) 38} \\ 0 \overline{) 30} \\ \hline 1 \overline{) 06} \end{array}$$

C

Exam.

Exam. II. Suppose another small vessel, whose length is ynches 30 and 7 tenth parts, *viz.* 30 $\frac{7}{10}$, and the diameter at the bung 34 hundredth parts of a gallon: and the diameter at the head 28 hundredth parts. what is the content?

Adde the two diameters together, that at the bung being doubled: the summe is onely 96 hundredth parts of a gallon,
 by *Rule II.* Multiply
 this summe by the
 length 30 $\frac{7}{10}$: and the
 product shall be 291 $\frac{7}{10}$,
 by *Rule III*, that is gallons 29, and
 47 hundredth parts, which is almost
 an halfe. which is the true content.
 For the first figure 2 signifyeth not
 200 (though it be so marked on the
 line of denarie numbers) but only 20;
 as both plaine reason, & also the short
 rule, at the end of *Rule III*, wil shew.

Exam. III. Suppose a great vessel: whose length is ynches 70 and an halfe, *viz.* 70 $\frac{1}{2}$; and the diameter

er at the bung gallons 2 and 3 hundredreth parts, *viz.* $2\frac{103}{100}$; and the diameter at the head gallons 1 and 10 hundredreth parts, *viz.* $1\frac{10}{100}$. what is the content?

Add the two diameters together, that at the bung being doubled; the summe is gallons 5 and

16 hundredreth parts, by
Rule II. Multiply this
 summe by the length
 $70\frac{1}{2}$: but because the
 units place of the line of
 digit numbers, being

$$\begin{array}{r} 2\frac{103}{100} \\ 2\frac{103}{100} \\ 1\frac{10}{100} \\ \hline 5\frac{116}{100} \\ 2)5\frac{116}{100} \\ \hline 2\frac{58}{100} \end{array}$$

set to $70\frac{1}{2}$ in the line of denarie numbers, the summe of the diameters $5\frac{116}{100}$ will over-reach beyond the socket: therefore to helpe this, take halfe the summe of the diameters, *viz.* gallons $2\frac{58}{100}$: and multiply that halfe summe by the length $70\frac{1}{2}$: and the product shall bee $181\frac{39}{100}$, by *Rule III*, that is gallons 181 and almost 9 tenth parts: which is halfe the true content. And being doubled shall give gallons $363\frac{78}{100}$ for the whole content of that great vessell.

The

The Examples following are of some vessels measured in the presence of them, which were deputed by the Company of Vintners to see the tryall of this Gauging line or rod.

Exam. V. A Canarie pipe whose length was ynches 48 and an halfe, viz. $48\frac{1}{2}$; and the diameter at the bung 93 hundreth parts of a gallon, viz. $0\frac{93}{100}$; and the diameter at the head 54 hundreth parts, viz. $0\frac{54}{100}$. what is the content?

Add the two diameters together, that at the bung being doubled, the summe is
 gallons 2 and 4 tenth parts, by *Rule II.* Multiply this summe by the length $48\frac{1}{2}$: and the product shall bee $116\frac{1}{4}$ by *Rule III.* that is gallons 116 & 4 tenth parts: which is the content sought for.

Exam. VI. A Graves-hoghead whose length was ynches 31 and 3 tenth parts, viz. $31\frac{3}{10}$: And the diameter at the bung 73 hundreth parts of a gallon, viz. $0\frac{73}{100}$; and the diameter

(35)

meter at the head 57 hundreth parts,
viz. 0, 57. What is the content?

Adde the two dia-
meters together, that
at the bung being
doubled, the Summe
is gallon 2 and 3 hun-
dred parts, by Rule II. Multiply
this summe by the length 31, 2: and
the product shall bee 63, 4 by Rule
III, that is gallons 63 and 34 hun-
dred parts: which is the content
sought for.

$$\begin{array}{r} 0'73 \\ 0'73 \\ \hline 0'146 \\ \hline 2'10 \end{array}$$

Example VII. A High-countrey
hogthead whose length was ynches
30, and 82 hundreth parts, viz. 30, 82:
And the diameter at the bung 63 hun-
dred parts of a gallon: viz. 0, 63 and
the diameter at the head 51 hundreth
parts, viz. 0, 51. What is the con-
tent?

Adde the two diame-
ters together, that at
the bung being doub-
led, the summe is gal-
lons 1 and 77 hun-

$$\begin{array}{r} 0'63 \\ 0'63 \\ \hline 0'126 \\ \hline 1'77 \end{array}$$

C 3

dred

dreth parts, by Rule II. Multiply this summe by the length 30, ⁸²: and the product shall bee 54155, by Rule III, that is gallons 54 and 55 hundredth parts: which is the true content sought for.

The use of
this Instru-
ment in
gauging
beere ves-
sels.

Although this Gauging instrument is properly framed for measuring vessels by the wine gallon: yet it may also fitly be applyed to the measuring of the same vessels by the ale or beere gallon. And for this purpose I have on the Ruler figured with digit numbers set two little lines or markes, the one at 272 $\frac{1}{2}$, noted with the letter (w); and the other at 231, noted with the letter (a). The use of which I deliver in this Rule following.

Seeke out the content of the vessell proposed in wine gallons, upon the ruler figured with denarie numbers, as hath before beene taught: and thereto set the marke (w): and so shall the other marke (a) point to the number of beere gallons contained in the same vessell.

I will

I will shew the practice of this Rule by the vessells measured in the three last examples.

First The Canarie pipe, whose length was ynches $48\frac{1}{2}$: and the diameter at the bung gallon $0\frac{93}{100}$: and the diameter at the head gallon $0\frac{14}{100}$: the measure whereof was by Example V found to be gallons $116\frac{1}{4}$: how many beere gallons will it containe?

Set the marke (w) unto the wine measure $116\frac{1}{4}$ reconed upon the ruler figured with denarie numbers, scruing it there fast, and the marke (4) shall in the same ruler point out $98\frac{7}{8}$ that is gallons 98 and 76 hundredth parts, the content thereof in beere measure.

Againe, The Graves hogshead, whose length was ynches $31\frac{1}{2}$: and the diameter at the bung gallon $0\frac{73}{100}$: and the diameter at the head gallon $0\frac{57}{100}$: the measure whereof was by Example VI found to be gallons $63\frac{1}{4}$: how many beere gallons will it containe?

Set the marke (w) unto the wine
C 4 mea-

measure $631\frac{3}{4}$ recond upon the ruler figured with denarie numbers, scrving it there fast: and the marke (a) shall in the same Ruler point out $531\frac{7}{8}$, that is gallons 53, and 74 hundreth parts, the content thereof in beere measure.

Lastly the High countrey hoggehead, whose length was ynches $30\frac{8}{11}$: and the diameter at the bung gallon $01\frac{6}{11}$: and the diameter at the head gallon $01\frac{5}{11}$: the measure whereof was by Example VII found to bee gallons $54\frac{5}{11}$: how many beere gallons will it containe?

Set the marke (w) unto the wine measure $54\frac{5}{11}$ recond upon the ruler figured with denarie numbers, scrving it there fast: and the marke (a) shall in the same ruler point out $461\frac{8}{11}$, that is gallons 46, and 28 hundreth parts, the content thereof in beere measure.

And

And now I have finished what I determined to write concerning the use of this my *new Gauging line or rod*: and have made it so plaine and easie that I doubt not but every meane capacitie will bee able with a little care to apprehend the meaning and practice: I have also delivered the *Rule* which I follow, and where-upon I ground this worke: only the manner of computing the *Gauge-divisions* I have concealed: both because that speculation is impertinent to the managing and hand-working therewith: and also that because unto men of art by comparing the rule with the performance, it will not bee difficult to find out the reason: but especially because I intend and wish the benefit of making and fabricating this Instrument, unto Mr. *Elias Allen*, who gave the occasion of it, and at whose request I invented it. And if it shall bee serviceable to this most illustrious Citie, as a meanes of keeping truth and equitie in that kind, and acceptable to you Right Honourable

table LL, and to you Right Worship-
full to whom I present it, and con-
ducing unto the glory of Al-
mighty God, the author of
every good abilitie, it hath
obtaind the desired

END.

Addition	} <i>find out</i>	{ the summe or aggregate.
Subduction		{ the remaines or difference
Multiplicon		{ the product or rectangle.
Division		{ the quotient.

Perlegi hac opus Mathematicum,
cui titulus est, The new artific-
all Gauging Line or Rod, in quo
nihil reperio quod non cum utilitate
publica imprimatur, modo intra tres
menses proximè sequentes Typis man-
datur.

Ex edibus Lambethanis,

Octob. 10.

1633.

Guil. Bray.

17
14/10/16

THese Instruments are
made in brasse by
Elias Allen over against
St. Clements Church with-
out Temple-barre : where
also those who are desirous
may bee instructed in the
practicall use thereof: and
such as shall have occasion
may have vessels gauged.

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